Crystal Structure, Mössbauer Spectra, Thermal Expansion, and Phase Transition of Berthierite FeSb₂S₄

K. Łukaszewicz,*¹ A. Pietraszko,* J. Stępień-Damm,* A. Kajokas,† J. Grigas,† and H. Drulis*

*Institute of Low Temperature and Structure Research, Polish Academy of Sciences, Okólna 2, 250-422 Wrocław, Poland; and †Department of Physics, University of Vilnius, Sauletekio al. 9/3, 2040 Vilnius, Lithuania

Received Jauary 25, 2001; in revised form July 30, 2001; accepted August 9, 2001

Dielectric and ultrasound measurements of berthierite FeSb₂S₄ reported in the literature revealed a phase transition at $T_{\rm c} = 348$ K. In the present study the phase transition was confirmed by Mössbauer spectra exhibiting anomalous behavior close to 350 K. Precise lattice parameters measured in the temperature region 305-380 K show a change of slope at about 350 K. The crystal structure of FeSb₂S₄ has been determined using single-crystal X-ray diffraction data at both room temperature and 370 K above the phase transition. The crystal structure is orthorhombic, Z = 4. At 295 K a = 11.412(2) Å, b =3.763(1)Å, c = 14.161(3)Å, and R = 0.0280, and at 370 K a = 11.421(2)Å, b = 3.771(1)Å, c = 14.173(3)Å, and R =0.0274. No symmetry change has been observed. At both temperatures the space group of FeSb₂S₄ is *Pnma* with small changes in atomic parameters and interatomic distances. The transition observed at 348 K is, therefore, to be classified as a weak phase transition going on without essential changes in the crystal structure. © 2001 Academic Press

Key Words: FeSb₂S₄; berthierite; Mössbauer spectra; thermal expansion; crystal structure; weak phase transition.

INTRODUCTION

The crystal structure of berthierite FeSb_2S_4 at ambient temperature had been first determined and refined in the space group *Pnma* in 1955 by Buerger and Hahn (1). New refinements (2, 3) confirmed previous results with small changes in structure parameters. The problem of the crystal structure and symmetry of berthierite remains nevertheless still open. Grigas and co-workers (4, 5) found that the crystal of FeSb_2S_4 was a semiconductor with both high electric conductivity and dielectric permittivity. Needle-shaped berthierite crystals show along the *b* axis (parallel to the needle axis) an anomalous dependence of permittivity and electric conductivity on temperature. A jump of both ε and $tg \delta$ has

 $^1\mathrm{To}$ whom correspondence should be addressed. E-mail: kl@int. pan.wroc.pl.

been observed at 348 K. The phase transition of berthierite has been confirmed by the measurements of temperature dependence of attenuation of longitudinal ultrasound along the *b* axis (5). At microwaves the dielectric permittivity follows the Curie–Weiss law with the Curie temperature $T_c = 348$ K and the Curie–Weiss constant $C = 1.2 \times 10^3$ K (6).

The present study was aimed at explaining the nature of the phase transition observed in (4, 5) and checking the crystal structure of berthierite at both an ambient temperature and 370 K, well above the expected phase transition temperature.

EXPERIMENTAL

Data were collected at ambient temperature T = 295 K and at T = 370 K by the KUMA-Diffraction KM4 diffractometer with graphite-monochromated MoK α radiation $(\lambda = 0.71073 \text{ Å})$. Precise lattice parameters were determined as a function of temperature by the Bond method (7) developed in our laboratory for precise measurements of the thermal expansion of single crystals (8). Intensities were measured with the ω/θ scan technique with a scan speed depending on intensity. No significant intensity variation was observed for two standard reflections. The reflection intensities were corrected for the Lorentz and polarization effects. Empirical absorption correction was applied based on Ψ scans for selected reflections. The extinction correction was introduced in the full-matrix least-squares refinement on F^2 performed by using the SHELXL-97 program (9). Preliminary atomic positions were taken from (3).

The ⁵⁷Fe Mössbauer spectra were taken at several temperatures in the range of 295–385 K with a conventional constant acceleration spectrometer. The source was ⁵⁷Co in an Rh matrix. The velocity scale calibration and the isomer shift values estimation have been performed relative to Na₂(NO)Fe(CN)₅ · 2H₂O.

Crystal data and details of the refinement procedure are presented in Table 1. Weighted R factors wR_2 and goodness



1000204 4					
Chemical formula weight	427.59				
Ζ	4				
F(000)	768				
Wavelength, $MoK\alpha(Å)$	0.71073				
Crystal system	Orthorhombic	rthorhombic			
Crystal shape and size	Needles, approximately 0.24×0.03 $\times 0.03$ mm				
Absorption correction	Ψ scan				
Data collection: KUMA-Diffracti with prescanning	ion KM-4 diffractor	meter, ω/θ scan			
θ range for data collection (°)	2-30				
Reflections 303 and $02\overline{3}$ monitore variation $<1\%$	ed every 50 reflection	ons, intensity			
Unit cell dimensions from indepen	ndent thermal expa	nsion measurements			
Temperature (K)	295	370			
$a(\text{\AA})$	11.412(2)	11.421(2)			
$b(\mathbf{A})$	3.763(1)	3.771(1)			
c(Å)	14.161(3)	14.173(3)			
$V(Å^3)$	608.1(2)	610.4(2)			
Density D_x (mg/m)	4.670	4.653			
Absorption coefficient (mm ⁻¹)	12.404	12.358			
Space group	Pnma	Pnma			
Index ranges: h	$-16 \rightarrow 16$	$-16 \rightarrow 16$			
k	$-5 \rightarrow 0$	$-3 \rightarrow 5$			
l	$-19 \rightarrow 19$	$-13 \rightarrow 19$			
Measured reflections	3483	2343			
Independent reflections, total	998	955			
R _{int}	0.0358	0.0295			
Observed reflections $[I > 2\sigma(I)]$	886	882			
Extinction coefficient	0.0027	0.0023			
Number of parameters	44	44			
$R_1 \left[I > 2\sigma(I) \right]$	0.0280	0.0274			
$wR_2(F^2) \left[I > 2\sigma(I)\right]$	0.0597	0.0640			
$(\Delta/\sigma)_{ m max}$	< 0.001	< 0.001			
$\Delta \rho_{\rm max} / \Delta \rho_{\rm min} \ ({\rm e} {\rm \AA}^{-3})$	1.34/-1.21	1.8/-1.8			
$\Delta ho_{ m max}$ at	0.66Å from Sb1	0.81 Å from Sb2			

 TABLE 1

 Crystal Structure Determination Data for Berthierite

 FeSb₂S₄ at 295 and 370 K

of fit S are based on F^2 and conventional R_1 factor based on F_0 , with F_0 set to zero for negative F_0^2 .

RESULTS AND DISCUSSION

Mössbauer spectra at RT and 378 K are presented in Fig. 1. The hyperfine parameters, the quadrupole splitting, QS, and the isomer shift, IS, have been calculated by the least-squares fits of the experimental results within the Lorentz approximation for one doublet coming from the studied sample and another one from the furnace holder. In spite of this, the parameters estimated at 295 K are in good agreement with those reported in earlier Mössbauer studies (10) where only one quadrupole doublet had been observed (there were no impurity subspectra).

The temperature dependencies of QS and IS of the Fe nucleus are shown in Fig. 2. Both parameters exhibit anomalous behaviors at temperatures close to 350 K. Such



FIG. 1. The Mössbauer spectra of $FeSb_2S_4$ at temperatures (a) 295 K and (b) 378 K. A small doublet visible in the central part of the spectra comes from the furnace holder.

changes in the QS and IS parameters are usually observed when the material undergoes the phase transition induced by the temperature or by the pressure. From the Mössbauer data it appears that the $FeSb_2S_4$ undergoes apparently in the temperature range 323–365 K a structural phase transition of second order. Nevertheless, we cannot confirm the symmetry change connected with the phase transition at 348 K as suggested in (4). In such a case, in the phase of

F

S

S

F

S

5 5 5

S



FIG. 2. (a) The isomer shift and (b) the quadrupole splitting of 57 Fe Mössbauer spectra of FeSb₂S₄ as a function of temperature.

lower symmetry we would observe two superimposed doublets in Mössbauer spectra connected with two nonequivalent Fe atoms. The attempts, however, to analyze the Mössbauer spectra with two doublets have failed. A narrow line with almost the same linewidth ($\Gamma = 0.28$ mm/s) at both room temperature and 378 K justifies the description of Mössbauer spectra with a single quadrupole doublet. In the frame of our experimental accuracy it appears that the phase transition observed in FeSb₂S₄ at 348 K is isostructural with no symmetry change.

Figure 3 shows lattice parameters and lattice volume of $FeSb_2S_4$ as a function of temperature. Each parameter exhibits a small change in slope at about 350 K manifested as an anomaly of thermal expansion, indicating weak phase transition of second order. The crystal structure of $FeSb_2S_4$ at both room temperature and 370 K was refined in the

 $\begin{array}{c} {\rm TABLE\ 2}\\ {\rm Atomic\ Coordinates\ and\ Equivalent\ Isotropic\ Displacement}\\ {\rm Parameters\ }U_{\rm eq}\ for\ FeSb_2S_4 \end{array}$

tom	Site	x	У	Ζ	$U_{ m eq}$	
		T =	295 K			
⁷ e	4c	0.31673(6)	0.25	0.66495(5)	0.0164(2)	
b1	4c	0.14473(3)	0.25	0.93684(2)	0.0177(1)	
b2	4 <i>c</i>	0.03882(3)	0.25	0.38563(2)	0.0144(1)	
1	4c	0.8045(1)	0.25	0.27030(8)	0.0150(2)	
2	4c	0.4220(1)	0.25	0.81593(9)	0.0164(2)	
3	4c	0.2234(1)	0.25	0.50584(9)	0.0152(2)	
4	4 <i>c</i>	0.5494(1)	0.25	0.40456(8)	0.0150(2)	
		T =	370 K			
Fe	4c	0.31639(7)	0.25	0.66506(6)	0.0207(2)	
b1	4c	0.14453(3)	0.25	0.93692(3)	0.0219(1)	
b2	4c	0.96087(3)	0.25	0.38547(3)	0.0178(1)	
1	4c	0.8042(1)	0.25	0.2700(1)	0.0187(3)	
2	4c	0.4226(1)	0.25	0.8160(1)	0.0205(3)	
3	4c	0.2235(1)	0.25	0.5060(1)	0.0191(3)	
4	4 <i>c</i>	0.5491(1)	0.25	0.4046(1)	0.0177(3)	
						_

centrosymmetric space group *Pnma* and in four orthorhombic subgroups of *Pnma*: $P2_12_12_1$, $Pmn2_1$, $Pna2_1$, and $Pmc2_1$. In all cases the discrepancy indices *R* were satisfactory. The is no reason, therefore, to assume the polar space group, though in the high-temperature phase slightly better agreement between F_o an F_c was obtained for the space group $Pmn2_1$. Atomic parameters for FeSb₂S₄ at both temperatures are listed in Table 2.

Figure 4 shows a perspective view of FeSb_2S_4 along [010]. The three-dimensional framework consists of two polyhedral types: [FeS₆] octahedra and [SbS₅] orthorhombic pyramids. Bond distances and angles for the polyhedra are listed in Table 3. By sharing two opposite edges, Fe octahedra form infinite chains (FeS₄)⁶ⁿ⁻_n running parallel to the [010] axis. The Sb³⁺ cations are inserted between the chains inside an orthorhombic pyramid (Fig. 5). Both Figs. 4 and 5 were prepared by using the program in (11). The Sb1 cations are attached to (FeS₄)⁶ⁿ⁻_n chains by short Sb1–S3 and Sb1–S4 bonds. The chains joined by Sb2 form layers perpendicular to [001]. It is worth noting a slight external shift of the Sb1 position in relation to the base of the pyramid, whereas Sb2 remains in the plane of the base of the pyramid.

In semiconductors with a great amount of covalency, such as berthierite, the electronic subsystem plays an important role in a delicate balance of short- and long-range interactions (6). One can assume that even the small changes in the lattice significantly disturb the electronic subsystem, inducing spontaneous polarization and the anomalies of semiconductive and dielectric properties. It appears, therefore, that the observed phase transition in $FeSb_2S_4$ semiconductor is mostly related to the electronic subsystem.



FIG. 3. Lattice parameters a, b, and c and lattice volume V of FeSb₂S₄ as a function of temperature. Superimposed second derivatives indicate a change in slope.



FIG. 4. Perspective view of the crystal structure of ${\rm FeSb_2S_4}$ along [010] with $[{\rm FeS_6}]$ octahedra.

FIG. 5. Perspective view of the crystal structure of ${\rm FeSb}_2S_4$ along [010] with $[{\rm SbS}_5]$ pyramids.

Main I	nteratomic	Distance	es (Å) an	d Angles	(°) in FeS	Sb ₂ S ₄	
Fe	S2	S3	S 1	S 1	S4	S4	
			T = 295 K	-			
	F	Fe octahed	ron, site s	ymmetry: <i>n</i>	1		
S2	2.453(2)	4.942(2)	3.422(1)	3.422(1)	3.660(2)	3.660(2)	
S3	175.97(4)	2.492(2)	3.700(2)	3.700(2)	3.446(1)	3.446(2)	
S1	87.22(4)	94.44(4)	2.509(2)	3.763(1)	3.477(2)	5.123(1)	
S1	87.22(4)	95.44(4)	97.18(4)	2.509(2)	5.123(1)	3.477(2)	
S4	92.40(4)	84.81(3)	85.42(3)	177.35(4)	2.616(1)	3.763(1)	
S4	92.40(4)	84.81(3)	177.35(4)	85.42(3)	91.97(3)	2.616(1)	
		〈 Fe	$\langle -S \rangle = 2.5$	33 Å			
	Sb1 pyramid			Sb2 pyramid			
Sb1-S4		2.496(1)		Sb2-S1	2.4	2.422(1)	
Sb1-S3		2.600(1)	Sb2-S2	2.508(1)		
Sb1-S4		2.600(1)	Sb2-S1	2.508(1)		
Sb1-S4		2.942(1)	Sb2-S1	3.215(1)		
Sb1-S4		2.942(1)	Sb2-S1	Sb2–S1 3.215(1)		
	$\langle Sb-S \rangle = 2$	2.716 Å		$\langle \mathrm{Sb-S} angle = 2.774\mathrm{\AA}$			
			T = 370 K	ĩ			
	F	Fe octahed	ron, site s	ymmetry: <i>n</i>	1		
Fe	S2	S3	S1	S 1	S4	S4	
S2	2.458(2)	4.946(2)	3.687(1)	3.687(1)	3.665(2)	3.665(2)	
S3	175.65(64)	2.491(2)	3.706(2)	3.706(2)	3.450(1)	3.450(2)	
S1	87.24(4)	95.62(4)	2.510(2)	3.771(2)	3.482(2)	5.133(1)	
S1	87.24(4)	95.62(4)	97.40(6)	2.510(2)	5.133(1)	3.384(2)	
S4	92.21(4)	84.76(4)	85.38(3)	177.14(4)	2.625(2)	3.771(2)	
S4	92.21(4)	84.76(3)	177.14(4)	85.38(3)	91.84(3)	2.625(1)	
		<fe< td=""><td>$\langle -S \rangle = 2.5$</td><td>37 Å</td><td></td><td></td></fe<>	$\langle -S \rangle = 2.5$	37 Å			
	Sb1 pyramid			Sb2 pyramid			
Sb1-S4	2.496(2)		Sb2-S1	2.425(1)			
Sb1-S3	2.605(1)		Sb2-S2	2.510(1)			
Sb1-S4	2.605(1))	Sb2-S1	2.510(1)		
Sb1-S4		2.942(1)		Sb2-S1	3.218(1)		
Sb1-S4		2.942(1)	Sb2-S1	3.2	218(1)	
	$\langle Sb-S \rangle = 2.718 \text{ Å}$			$\langle Sb-S \rangle = 2.776 \text{ Å}$			

TADIE 2

Supplementary data including anisotropic temperature factors and lists of structure factors may be obtained upon request from the authors.

ACKNOWLEDGMENT

The authors are indebted to Mr. P. Gaczyński for performing Mössbauer measurements.

REFERENCES

- 1. M. J. Buerger and T. Hahn, Am. Mineral. 40, 226 (1955).
- 2. K. Bente and A. Edenharter, Z. Kristallogr. 187, 31 (1989).
- 3. P. Lemoine, D. Carre, and F. Robert, Acta Crystallogr. C 47, 938 (1991).
- J. Grigas, A. Orliukas, and N. N. Mozgova, *Lietuvos Fiz. Rinkinys* 15, 872 (1975).
- 5. J. Grigas, Ferroelectrics 20, 173 (1978).
- J. Grigas, "Microwave Dielectric Spectroscopy of Ferroelectrics and Related Materials." Gordon & Breach, New York, 1996.
- 7. W. L. Bond, Acta Crystallogr. 13, 814 (1960).
- D. Kucharczyk, A. Pietraszko, and K. Łukaszewicz, J. Appl. Crystallogr. 26, 467 (1993).
- 9. G. M. Sheldrick, SHELXL-97: A Program for Crystal Structure Refinement, Univ. of Goettingen, Germany, 1997.
- P. Bonville, C. Garcin, A. Gérard, P. Imbert, and M. Wintenberger, Hyperfine Interaction 52, 279 (1989).
- K. Brandenburg, Diamond Version 2.1d, Crystal Impact GbR, Created Nov 16, 2000, Serial no. 9-48100.